

Condense each expression to a single logarithm.

34)  $5 \log_4 u$

$$= \log_4 u^5$$

35)  $\log_6 a - \log_6 b$

$$= \log_6 \left( \frac{a}{b} \right)$$

36)  $\log_3 a + \log_3 b$

$$= \log_3 (ab)$$

37)  $4 \log_4 u + 4 \log_4 v$

$$\begin{aligned} &= \log_4 u^4 + \log_4 v^4 \\ &= \log_4 (u^4 v^4) \\ &\quad \text{or} \\ &= \log_4 (uv)^4 \end{aligned}$$

38)  $\log_5 x - 5 \log_5 y$

$$\begin{aligned} &= \log_5 x - \log_5 y^5 \\ &= \log_5 \left( \frac{x}{y^5} \right) \end{aligned}$$

39)  $5 \log_5 a + 5 \log_5 b$

$$\begin{aligned} &= \log_5 a^5 + \log_5 b^5 \\ &= \log_5 (a^5 b^5) \\ &\quad \text{or} \\ &= \log_5 (ab)^5 \end{aligned}$$

40)  $3 \log_2 w + 3 \log_2 u + 12 \log_2 v$

$$\begin{aligned} &= \log_2 w^3 + \log_2 u^3 + \log_2 v^{12} \\ &= \log_2 (w^3 u^3 v^{12}) \\ &\quad \text{or} \\ &= \log_2 (wuv^4)^3 \end{aligned}$$

41)  $4 \ln u + 8 \ln v + 4 \ln w$

$$\begin{aligned} &= \ln u^4 + \ln v^8 + \ln w^4 \\ &= \ln (u^4 v^8 w^4) \\ &\quad \text{or} \\ &= \ln (uv^2 w)^4 \end{aligned}$$

42)  $3 \ln a - \ln c - 6 \ln b$

$$\begin{aligned} &= \ln a^3 - \ln c - \ln b^6 \\ &= \ln \left( \frac{a^3}{cb^6} \right) \end{aligned}$$

Solve each equation.

43)  $-8 \cdot 10^p = -99$

$$10^p = 12.375$$
$$\downarrow$$
$$\text{LOG } 12.375 = p$$
$$\boxed{1.093 = p}$$

45)  $-8e^{8-8m} = -94.8$

$$e^{8-8m} = 11.85$$
$$\downarrow$$
$$\ln 11.85 = 8-8m$$
$$2.472 = 8-8m$$
$$\boxed{.691 = m}$$

47)  $16^{r+2} + 2 = 75$

$$16^{r+2} = 73$$
$$\downarrow$$
$$\text{LOG } 73 = r+2$$
$$\frac{\text{LOG } 73}{\text{LOG } 16} = r+2$$
$$1.547 = r+2$$
$$\boxed{-.453 = r}$$

49)  $10 \log_9 x = 30$

$$\text{LOG}_9 x = 3$$
$$\downarrow$$
$$9^3 = x$$
$$\boxed{729 = x}$$

51)  $10 + \log_6(-7k-7) = 14$

$$\text{LOG}_6(-7k-7) = 4$$
$$\downarrow$$
$$6^4 = -7k-7$$
$$1296 = -7k-7$$
$$\boxed{-186.143 = k}$$

44)  $3 \cdot 11^{p+1} = 41$

$$11^{p+1} = 13.\bar{6}$$
$$\downarrow$$
$$\text{LOG } 13.\bar{6} = p+1$$
$$\frac{\text{LOG } 13.\bar{6}}{\text{LOG } 11} = p+1$$
$$1.091 = p+1$$
$$\boxed{-.091 = p}$$

46)  $18^{v-4} = 2$

$$\downarrow$$
$$\text{LOG } 2 = v-4$$
$$\frac{\text{LOG } 2}{\text{LOG } 18} = v-4$$
$$.240 = v-4$$
$$\boxed{4.240 = v}$$

48)  $6 \cdot 10^{4k} - 10 = 61$

$$6 \cdot 10^{4k} = 71$$
$$10^{4k} = 11.8\bar{3}$$
$$\downarrow$$
$$\text{LOG } 11.8\bar{3} = 4k$$
$$1.073 = 4k$$
$$\boxed{.268 = k}$$

50)  $-3 + \ln(x+2) = 0$

$$\ln(x+2) = 3$$
$$\downarrow$$
$$e^3 = x+2$$
$$20.086 = x+2$$
$$\boxed{18.086 = x}$$

52)  $\log_5(a-3) = 2$

$$\downarrow$$
$$5^2 = a-3$$
$$25 = a-3$$
$$\boxed{28 = a}$$

$$53) -7 \ln 2v = -28$$

$$\ln 2v = 4$$

↓

$$e^4 = 2v$$

$$54.598 = 2v$$

$$\boxed{27.299 = v}$$

$$54) 5 \log_7 4v - 3 = -13$$

$$5 \log_7 4v = -10$$

$$\log_7 4v = -2$$

↓

$$7^{-2} = 4v$$

$$.020 = 4v$$

$$\boxed{.005 = v}$$

$$55) \log(4x+3) = \log 5x$$

$$4x+3 = 5x$$

$$\boxed{3 = x}$$

$$56) \ln x + \ln 6 = 3$$

$$\ln(6x) = 3$$

↓

$$e^3 = 6x$$

$$20.086 = 6x$$

$$\boxed{3.348 = x}$$

$$57) \ln(x+5) - \ln x = 2$$

$$\ln\left(\frac{x+5}{x}\right) = 2$$

$$e^2 = \frac{x+5}{x}$$

$$7.389 = \frac{x+5}{x}$$

$$7.389x = x+5$$

$$6.389x = 5$$

$$\boxed{x = .783}$$

$$58) \log_6(x+2) + \log_6 10 = 2$$

$$\log_6[10(x+2)] = 2$$

$$\log_6(10x+20) = 2$$

↓

$$6^2 = 10x+20$$

$$36 = 10x+20$$

$$16 = 10x$$

$$\boxed{1.6 = x}$$

$$59) \ln 6 + \ln(3x-3) = 4$$

$$\ln[6(3x-3)] = 4$$

$$\ln(18x-18) = 4$$

↓

$$e^4 = 18x-18$$

$$54.598 = 18x-18$$

$$\boxed{4.033 = x}$$

$$60) \ln 9 - \ln(3-4x) = 5$$

$$\ln\left(\frac{9}{3-4x}\right) = 5$$

↓

$$e^5 = \frac{9}{3-4x}$$

$$148.413 = \frac{9}{3-4x}$$

$$148.413(3-4x) = 9$$

$$445.239 - 593.652x = 9$$

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$$\boxed{x = .735}$$