

FOIL and Division with Radicals - PRACTICE

Simplify.

$$\begin{aligned}
 1) (5\sqrt{2}-3)(-3\sqrt{2}-2) \\
 &= -15\sqrt{4} - 10\sqrt{2} + 9\sqrt{2} + 6 \\
 &= -15 \cdot 2 - 1\sqrt{2} + 6 \\
 &= -30 - \sqrt{2} + 6 \\
 &= \boxed{-24 - \sqrt{2}}
 \end{aligned}$$

$$\begin{aligned}
 2) (-3+4\sqrt{5})(1-4\sqrt{5}) \\
 &= -3 + 12\sqrt{5} + 4\sqrt{5} - 16\sqrt{25} \\
 &= -3 + 16\sqrt{5} - 16 \cdot 5 \\
 &= -3 + 16\sqrt{5} - 80 \\
 &= \boxed{-83 + 16\sqrt{5}}
 \end{aligned}$$

$$\begin{aligned}
 3) (-4\sqrt{3}-4)(-4\sqrt{3}+1) \\
 &= 16\sqrt{9} - 4\sqrt{3} + 4\sqrt{3} - 4 \\
 &= 16 \cdot 3 - 4 \\
 &= 48 - 4 \\
 &= \boxed{44}
 \end{aligned}$$

$$\begin{aligned}
 4) (5+3\sqrt{2})(-3+5\sqrt{2}) \\
 &= -15 + 25\sqrt{2} - 9\sqrt{2} + 15\sqrt{4} \\
 &= -15 + 16\sqrt{2} + 15 \cdot 2 \\
 &= -15 + 16\sqrt{2} + 30 \\
 &= \boxed{15 + 16\sqrt{2}}
 \end{aligned}$$

$$\begin{aligned}
 5) \frac{\sqrt{12}}{\sqrt{15}} \cdot \frac{\sqrt{15}}{\sqrt{15}} &= \frac{\sqrt{180}}{\sqrt{225}} = \frac{\sqrt{36 \cdot 5}}{15} \\
 &= \frac{6\sqrt{5}}{15} = \frac{2\sqrt{5}}{5}
 \end{aligned}$$

$$6) \frac{4}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{4\sqrt{3}}{\sqrt{9}} = \frac{4\sqrt{3}}{3}$$

$$7) \frac{\sqrt{4}}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{\sqrt{20}}{\sqrt{25}} = \frac{\sqrt{4 \cdot 5}}{5} = \frac{2\sqrt{5}}{5}$$

$$\begin{aligned}
 8) \frac{4\sqrt{5}}{2\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} &= \frac{4\sqrt{10}}{2\sqrt{4}} = \frac{4\sqrt{10}}{2 \cdot 2} \\
 &= \frac{4\sqrt{10}}{4} = \sqrt{10}
 \end{aligned}$$

$$\begin{aligned}
 9) \frac{3\sqrt{6}}{2\sqrt{15}} \cdot \frac{\sqrt{15}}{\sqrt{15}} &= \frac{3\sqrt{90}}{2\sqrt{225}} = \frac{3\sqrt{9 \cdot 10}}{2 \cdot 15} \\
 &= \frac{3 \cdot 3\sqrt{10}}{30} = \frac{9\sqrt{10}}{30} = \frac{3\sqrt{10}}{10}
 \end{aligned}$$

$$10) -\frac{4}{2\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = -\frac{4\sqrt{3}}{2\sqrt{9}}$$

$$= -\frac{4\sqrt{3}}{2 \cdot 3} = \boxed{\frac{4\sqrt{3}}{6}} = \boxed{-\frac{2\sqrt{3}}{3}}$$

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$$11) -\frac{3}{2+\sqrt{3}} \cdot \frac{2-\sqrt{3}}{2-\sqrt{3}} = -\frac{6-3\sqrt{3}}{4-2\sqrt{3}+2\sqrt{3}-\sqrt{9}}$$

$$= \frac{6-3\sqrt{3}}{4-\sqrt{9}} = \frac{6-3\sqrt{3}}{4-3} = \frac{6-3\sqrt{3}}{1}$$

$$= \boxed{6-3\sqrt{3}}$$

$$12) \frac{3}{3+\sqrt{2}} \cdot \frac{3-\sqrt{2}}{3-\sqrt{2}} = \frac{9-3\sqrt{2}}{9-3\sqrt{2}+3\sqrt{2}-\sqrt{4}}$$

$$= \frac{9-3\sqrt{2}}{9-\sqrt{4}} = \frac{9-3\sqrt{2}}{9-2} = \boxed{\frac{9-3\sqrt{2}}{7}}$$

$$13) \frac{3}{4+\sqrt{2}} \cdot \frac{4-\sqrt{2}}{4-\sqrt{2}} = \frac{12-3\sqrt{2}}{16-4\sqrt{2}+4\sqrt{2}-\sqrt{4}}$$

$$= \frac{12-3\sqrt{2}}{16-\sqrt{4}} = \frac{12-3\sqrt{2}}{16-2} = \boxed{\frac{12-3\sqrt{2}}{14}}$$

$$14) \frac{4}{2-3\sqrt{2}} \cdot \frac{2+3\sqrt{2}}{2+3\sqrt{2}} = \frac{8+12\sqrt{2}}{4+6\sqrt{2}-6\sqrt{2}-9\sqrt{4}}$$

$$= \frac{8+12\sqrt{2}}{4-9\sqrt{4}} = \frac{8+12\sqrt{2}}{4-9 \cdot 2}$$

$$= \frac{8+12\sqrt{2}}{4-18} = \boxed{\frac{8+12\sqrt{2}}{-14}} = \boxed{\frac{4+6\sqrt{2}}{-7}}$$

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