

HOW Reminders

• Preparedness:

- Be in the classroom when the bell rings
- Have something to write with, a calculator, and your notebook

Engagement:

- Have your phone and computer put away

Warm-Up

Find the vertex, axis of symmetry, and its max/min value.

$$1) y = -\frac{1}{4}(x + 7)^2 - 1$$

vertex: $(-7, -1)$

axis of symmetry: $x = -7$

max at: $y = -1$

$$2) 2x^2 + 16x + 29$$

vertex: $(-4, -3)$

axis of symmetry: $x = -4$

min at: $y = -3$

2.2 Notes – Part 3

Learning Targets:

- I can find the vertex, axis of symmetry, and x -intercepts of a parabola given its equation in intercept form.
- I can graph a parabola given its equation in intercept form.



Discover it

Algebra 2

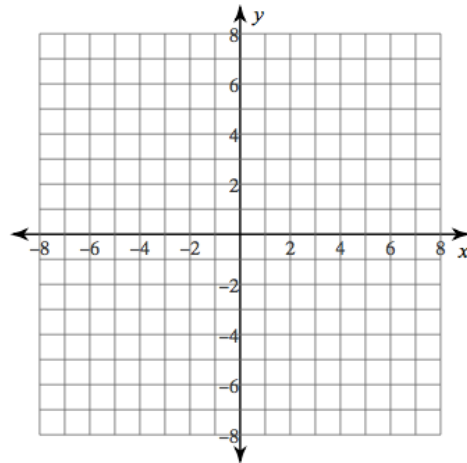
Name _____

Intercept Form

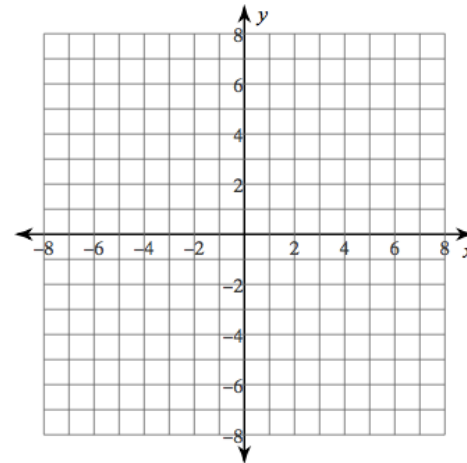
Date _____ Period _____

Graph each equation on Desmos. Record your discoveries. :)

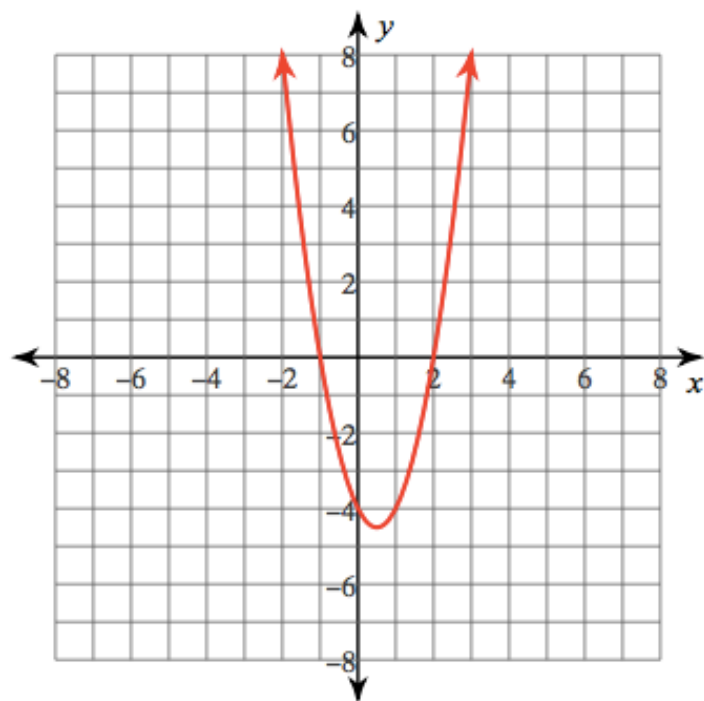
1) $f(x) = 2(x - 2)(x + 1)$



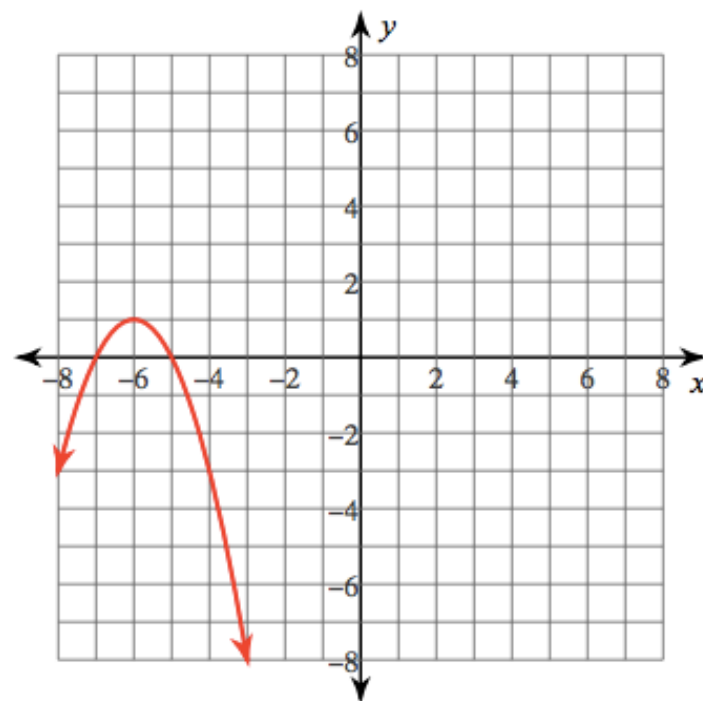
2) $f(x) = -(x + 7)(x + 5)$



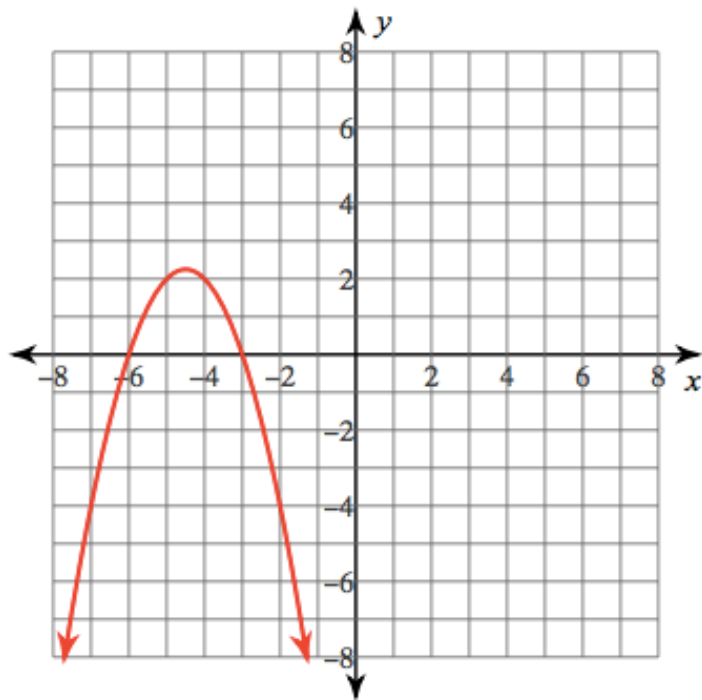
1) $f(x) = 2(x - 2)(x + 1)$



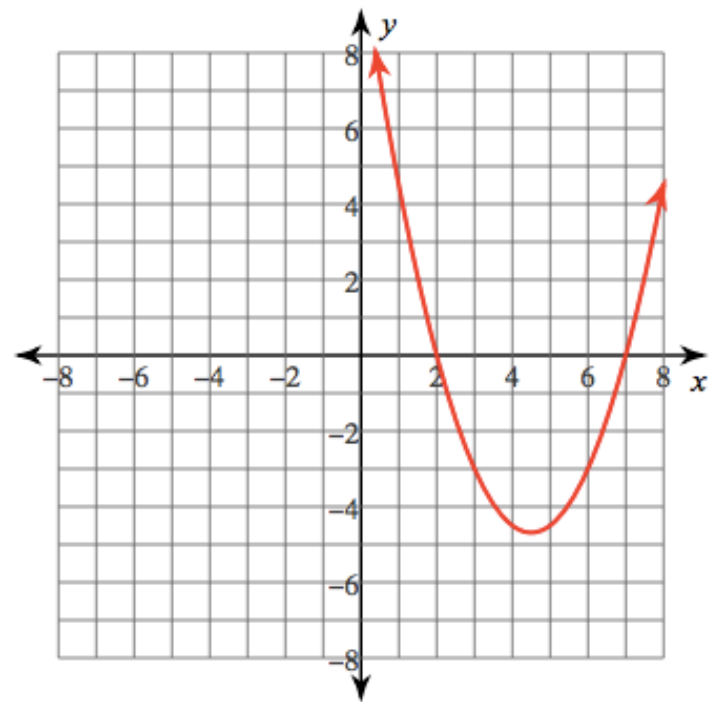
2) $f(x) = -(x + 7)(x + 5)$



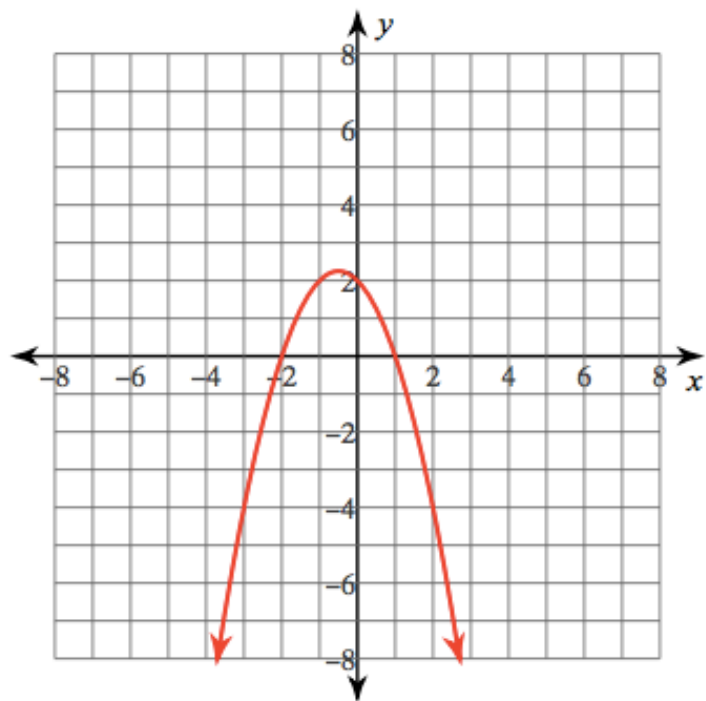
$$3) f(x) = -(x + 6)(x + 3)$$



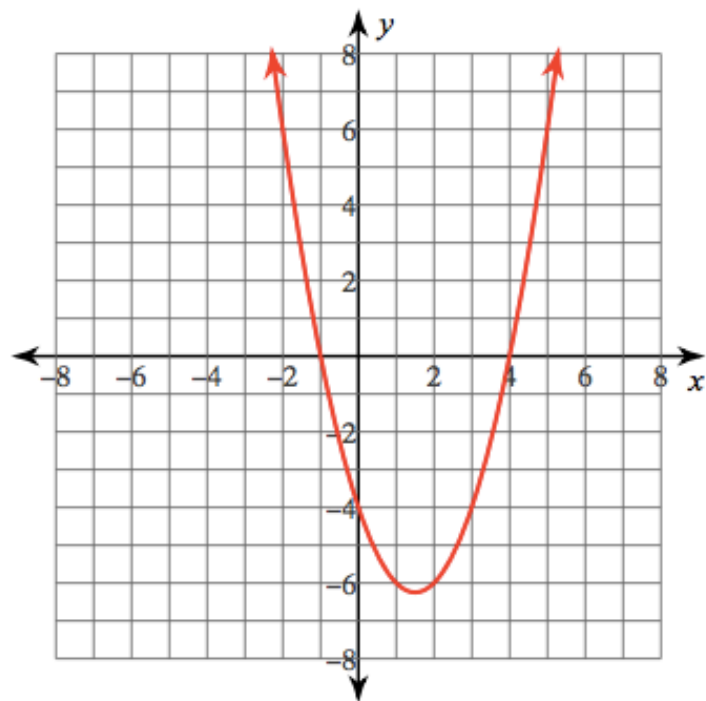
$$4) f(x) = \frac{3}{4}(x - 7)(x - 2)$$



5) $y = -(x - 1)(x + 2)$



6) $y = (x - 4)(x + 1)$



- **Vertex form:** $f(x) = -a(x - h)^2 + k$
 - vertex: (h, k)
 - axis of symmetry: $x = h$

- **Standard form:** $f(x) = ax^2 + bx + c$
 - vertex: $x = \frac{-b}{2a}$, plug in x to get y .
 - y -intercept = c



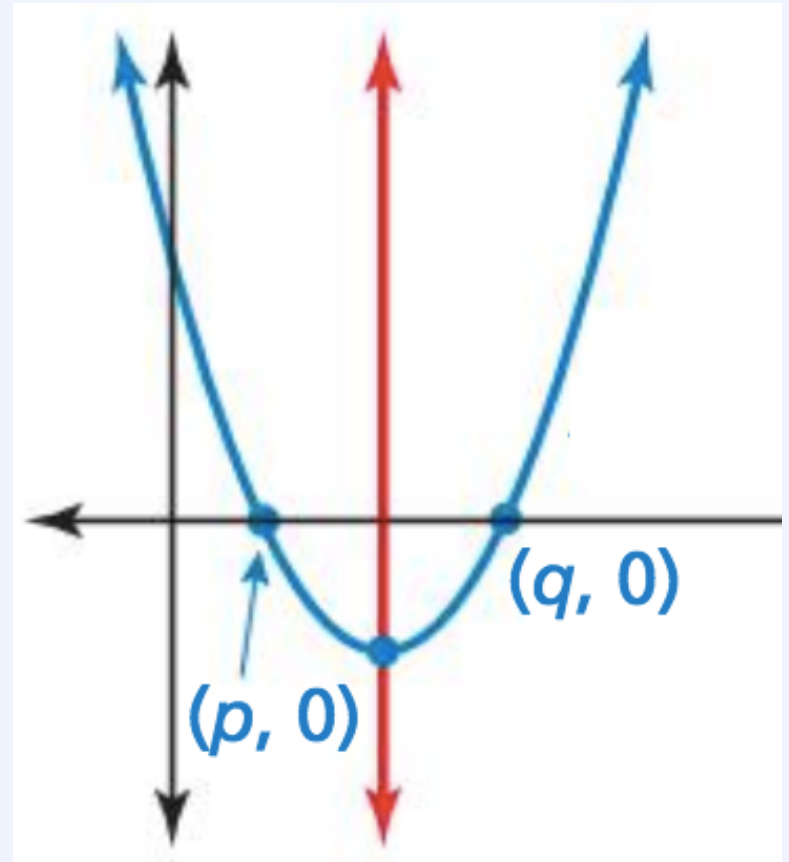
Intercept Form:

$$f(x) = a(x - p)(x - q)$$

Here, p and q are the x -intercepts of the parabola.

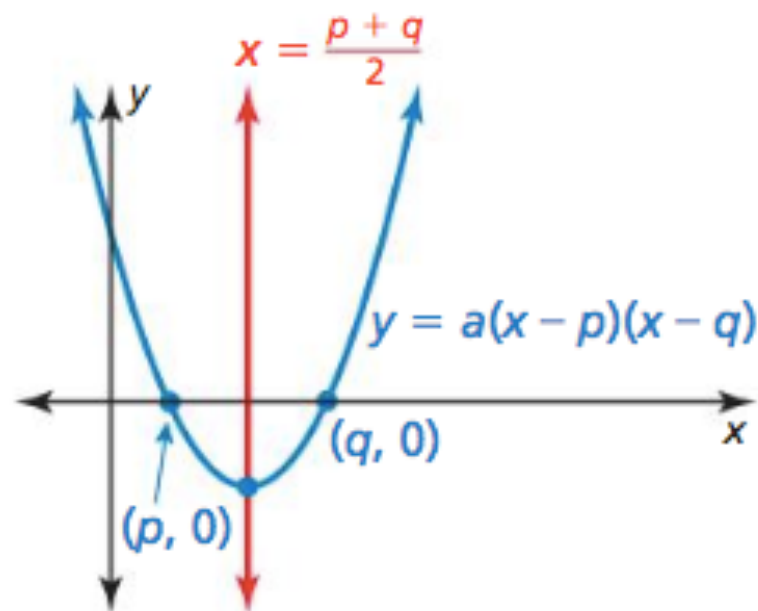
The the axis of symmetry is halfway between p and q , so:

$$x = \frac{p + q}{2}$$



Properties of the Graph of $f(x) = a(x - p)(x - q)$

- Because $f(p) = 0$ and $f(q) = 0$, p and q are the x -intercepts of the graph of the function.
- The axis of symmetry is halfway between $(p, 0)$ and $(q, 0)$. So, the axis of symmetry is $x = \frac{p + q}{2}$.
- The parabola opens up when $a > 0$ and opens down when $a < 0$.



Examples:

- 1) Graph $f(x) = -2(x + 3)(x - 1)$. Label the x -intercepts, vertex, and axis of symmetry.

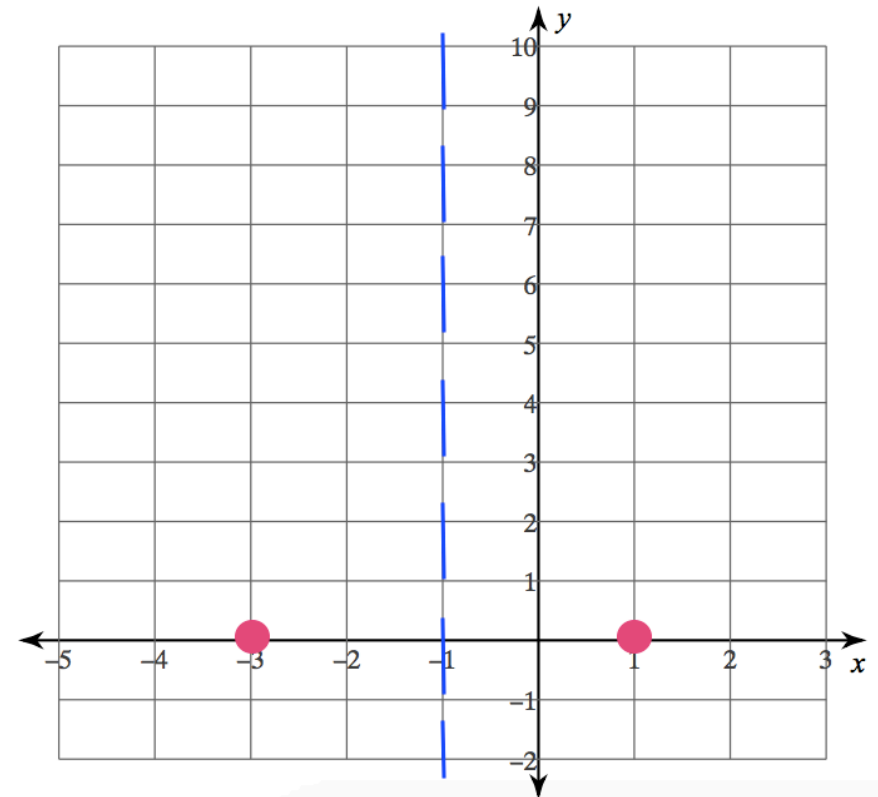
The x -intercepts are: $x = -3$ and $x = 1$

So, the axis of symmetry is:

$$x = \frac{-3 + 1}{2}$$

$$x = \frac{-2}{2}$$

$$x = -1$$



Examples:

- 1) Graph $f(x) = -2(x + 3)(x - 1)$. Label the x -intercepts, vertex, and axis of symmetry.

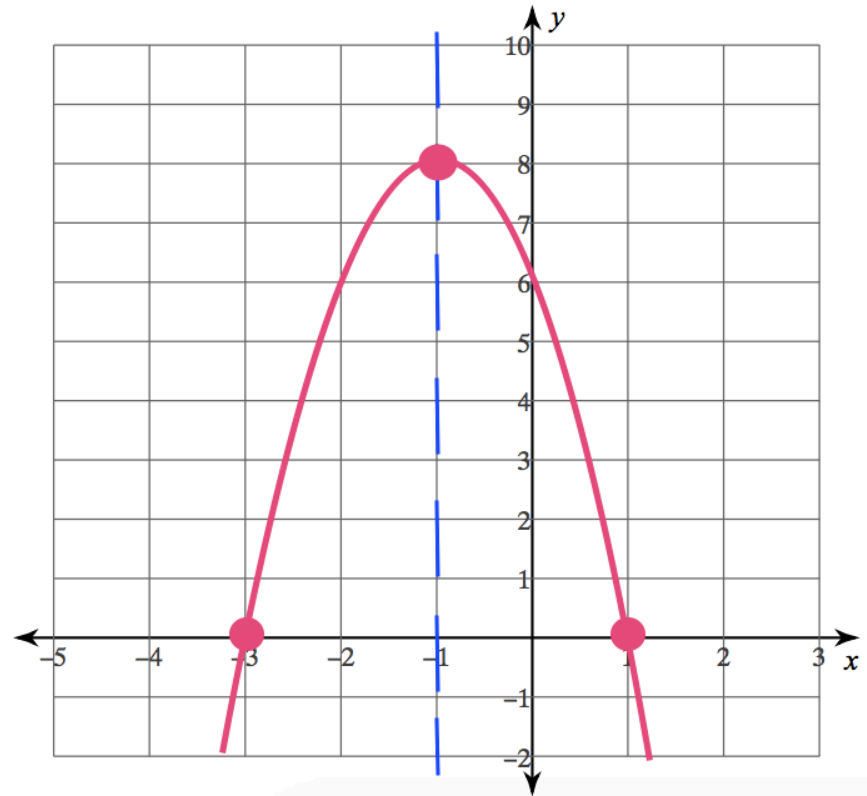
To find the vertex, plug $x = -1$, into the original equation.

$$f(-1) = -2(-1 + 3)(-1 - 1)$$

$$f(-1) = -2(2)(-2)$$

$$f(-1) = -4(-2)$$

$$f(-1) = 8 \quad \longrightarrow \quad \text{Vertex: } (-1, 8)$$



Examples:

2) Graph $f(x) = -(x + 1)(x + 5)$. Label the x -intercepts, vertex, and axis of symmetry.

3) Graph $g(x) = \frac{1}{4}(x - 6)(x - 2)$. Label the x -intercepts, vertex, and axis of symmetry.

Examples:

2) Graph $f(x) = -(x + 1)(x + 5)$. Label the x -intercepts, vertex, and axis of symmetry.

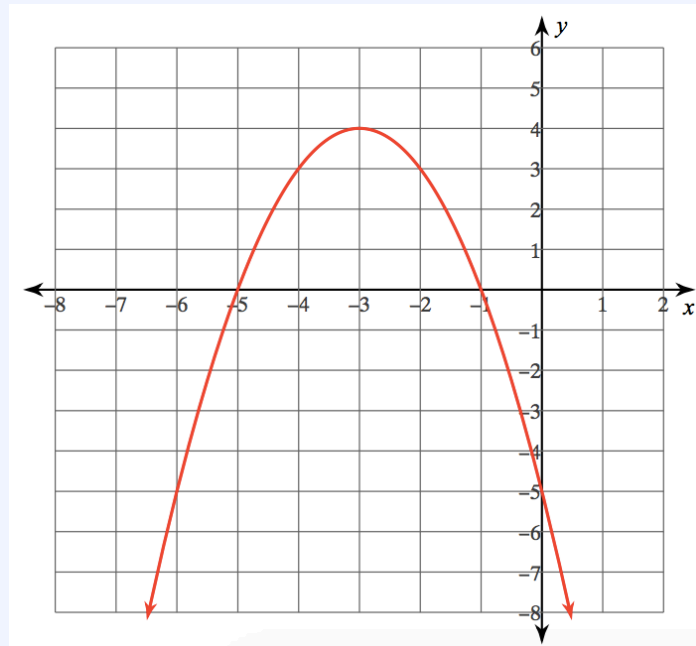
x -intercepts: $x = -1, x = -5$

vertex: $(-3, 4)$

$$\begin{aligned} f(-3) &= -(-3 + 1)(-3 + 5) \\ &= -(-2)(2) \\ &= (2)(2) \\ &= 4 \end{aligned}$$

axis of symmetry: $x = -3$

$$x = \frac{-1 + -5}{2} = \frac{-6}{2} = -3$$



Examples:

3) Graph $g(x) = \frac{1}{4}(x - 6)(x - 2)$. Label the x -intercepts, vertex, and axis of symmetry.

x -intercepts: $x = 6, x = 2$

vertex: $(4, -1)$

$$\begin{aligned} f(4) &= \frac{1}{4}(4 - 6)(4 - 2) \\ &= \frac{1}{4}(-2)(2) \\ &= \left(-\frac{1}{2}\right)(2) \\ &= -1 \end{aligned}$$

axis of symmetry: $x = 4$

$$x = \frac{6 + 2}{2} = \frac{8}{2} = 4$$

