

Finding ALL Solutions for sin & cos (NOTES)

Date _____ Period _____

Find all solutions to each equation in degrees.

$$1) \frac{-8 + \sqrt{2}}{2} = -4 + \cos \theta \text{ PER }= 360^\circ$$

$$\frac{\sqrt{2}}{2} = \cos \theta$$

$$\cos^{-1}\left(\frac{\sqrt{2}}{2}\right) = \theta$$

$$45^\circ = \theta$$

$$360^\circ - 45^\circ = 315^\circ$$

$$\begin{aligned} \theta &= 45^\circ + 360^\circ n \\ \theta &= 315^\circ + 360^\circ n \end{aligned}$$

$$2) \frac{10 - \sqrt{3}}{2} = 5 + \cos 2\theta \text{ PER }= 180^\circ$$

$$\frac{-\sqrt{3}}{2} = \cos 2\theta$$

$$\cos^{-1}\left(-\frac{\sqrt{3}}{2}\right) = 2\theta$$

$$150^\circ = 2\theta$$

$$75^\circ = \theta$$

$$180^\circ - 75^\circ = 105^\circ$$

$$\theta = 75^\circ + 180^\circ n$$

$$\theta = 105^\circ + 180^\circ n$$

$$3) \frac{8 \sin \theta}{2} = -4 \text{ PER }= 360^\circ$$

$$\sin \theta = -\frac{1}{2}$$

$$\theta = \sin^{-1}\left(-\frac{1}{2}\right)$$

$$\theta = -30^\circ$$

$$180^\circ - (-30^\circ) = 210^\circ$$

$$\begin{aligned} \theta &= -30^\circ + 360^\circ n \\ \theta &= 210^\circ + 360^\circ n \end{aligned}$$

$$4) -3 + \sin -2\theta = -\frac{5}{2} \text{ PER }= -180^\circ$$

$$\begin{matrix} \times 3 \\ +3 \end{matrix}$$

$$\sin -2\theta = \frac{1}{2}$$

$$-2\theta = \sin^{-1}\left(\frac{1}{2}\right)$$

$$-2\theta = 30^\circ$$

$$\theta = -15^\circ$$

$$-90^\circ - (-15^\circ) = -75^\circ$$

$$\begin{aligned} \theta &= -15^\circ + 180^\circ n \\ \theta &= -75^\circ + 180^\circ n \end{aligned}$$

Find all solutions to each equation in radians.

5) $-3\cos \theta = -3 \text{ PER} = 2\pi$

$$\cos \theta = 1$$

$$\theta = \cos^{-1}(1)$$

$$\theta = 0\pi$$

$$2\pi - 0\pi = 2\pi$$

$$\theta = 0\pi + 2\pi n$$

or

$$\boxed{\theta = 2\pi n}$$

6) $-8\cos 4\theta = 4\sqrt{3} \text{ PER} = \pi/2$

$$\cos 4\theta = -\frac{\sqrt{3}}{2}$$

$$4\theta = \cos^{-1}\left(-\frac{\sqrt{3}}{2}\right)$$

$$4\theta = \frac{5\pi}{6}$$

$$\theta = \frac{5\pi}{24}$$

$$\frac{\pi}{2} - \frac{5\pi}{24} \rightarrow \frac{12\pi}{24} - \frac{5\pi}{24} = \frac{7\pi}{24}$$

$$\theta = \frac{5\pi}{24} + \frac{\pi}{2}n$$

$$\theta = \frac{7\pi}{24} + \frac{\pi}{2}n$$

7) $-\frac{5}{2} = -2 + \sin \theta \text{ PER} = 2\pi$
 $\downarrow +2$

$$-\frac{1}{2} = \sin \theta$$

$$\sin^{-1}\left(-\frac{1}{2}\right) = \theta$$

$$\boxed{-\frac{\pi}{6} = \theta}$$

$$\pi - \frac{\pi}{6} \rightarrow \frac{5\pi}{6} - \frac{\pi}{6} = \boxed{\frac{4\pi}{6}}$$

$$\theta = -\frac{\pi}{6} + 2\pi n$$

$$\theta = \frac{7\pi}{6} + 2\pi n$$

8) $-3\sqrt{3} = 6\sin 2\theta \text{ PER} = \pi$

$$-\frac{\sqrt{3}}{2} = \sin 2\theta$$

$$\sin^{-1}\left(-\frac{\sqrt{3}}{2}\right) = 2\theta$$

$$-\frac{\pi}{3} = 2\theta$$

$$\boxed{-\frac{\pi}{6} = \theta}$$

$$\frac{\pi}{2} - \frac{\pi}{6} \rightarrow \frac{3\pi}{2} - \frac{\pi}{6} = \frac{4\pi}{6} = \boxed{\frac{2\pi}{3}}$$

$$\theta = -\frac{\pi}{6} + \pi n$$

$$\theta = \frac{2\pi}{3} + \pi n$$